Identifying multiple regimes in the model of credit to households

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Abstract

This research proposes a new method to identify the differing states of the market with respect to lending to households. We use an econometric multi-regime regression model where each regime is associated with a different economic state of the credit market (i.e. a normal regime or a boom regime). The credit market alternates between regimes when some specific variable increases above or falls below the estimated threshold level. A new method for estimating multi-regime threshold regression models for dynamic panel data is also demonstrated.

Keywords: credit boom, threshold regression, dynamic panel
JEL classification: E51, C23, C51
1. Introduction

Credit booms and busts have been responsible for much of the macroeconomic turbulence in emerging and developed markets. Lending booms are also known to be good predictors of banking and other financial crises (Kaminsky and Reinhart, 1999; Gourinchas, Valdes, and Landerrechte, 2001; Tornell and Westerman, 2002; Laeven and Valencia, 2008). Economists and policy makers often ask if credit grows too rapidly or too slowly given the actual state of the economy (Backé and Wójcik, 2008). Special attention is also paid to household loans that often initiate consumption, investment and production booms (Coricelli, Mucci, and Revoltella, 2006; Kiss, Nagy, Vonnák, 2006, Mendoza and Terrones, 2008).

Several studies aim to identify periods where credit was booming in different markets. For example, deviations from the long-run trend were used as a measure of the credit boom in some analyses (Mendoza and Terrones, 2008). Econometric error correction models were also employed to estimate the equilibrium level of credit and to assess possible divergence of credit levels from this equilibrium (Égert, Backé, and Zumer, 2006; Kiss, Nagy, and Vonnák, 2006, and references therein). However, the purely statistical methods used to calculate the long-run trend of credit, the Hodrick-Prescott filter, are not based on any economic foundation and therefore may fail to distinguish booms from normal credit growth in many emerging (catching-up) economies.

Error correction models do in fact take into account the economic long-run relationship between lending to households as well as other macroeconomic factors. The situation where credit deviates from this relationship is often regarded as evidence of a credit boom. However, some divergence from the equilibrium may be simply one-period episodes caused by some specific economic condition, policy, regulatory or accounting reform. An observation of credit over longer periods of time may reveal that although credit exceeds the sustainable level it follows the error correction mechanism and eventually returns to the
equilibrium state (Kiss, Nagy, and Vonnák, 2006). The movement of credit to households toward the long-run equilibrium should not be treated as a boom. Standard calculations will tend to overstate the number of boom periods where such return processes are not discarded.

On the other hand, the estimation of error correction parameters will be downward biased in the presence of prolonged booms because many observations will constitute upward deviations from the error correction mechanism. These biases will tend to understate the true number of booms in favor of returns to the equilibrium.

A suitable procedure is clearly needed to distinguish true booms from incidental deviations, returns, and catching-up processes as well as to eliminate the biases in the selection of boom regimes. In this paper we propose a new method to identify possible boom and bust regimes in the credit to households market. This new method deals with the problem of imprecise identification of boom episodes encountered in earlier studies by accounting for changing regimes in the credit market during different periods. Our approach relies on the economic interpretation of these regimes rather than on using estimates of deviations from long-run trends to detect periods of credit boom.

We assume that potential normal, boom, and bust periods can be identified as separate economic regimes. In normal times credit moves along the equilibrium path and deviates only slightly after minor disturbances. In turn, a credit boom is identified as a period (or regime) where credit does not follow macroeconomic fundamentals but instead it grows rapidly and departs from the long-run equilibrium. In the bust regime, credit falls back quickly to its equilibrium level.

We have constructed an econometric model where the impact of the explanatory variables on the growth rate of credit changes depends on the regime the model enters in a given period. This model is a multi-regime threshold regression where changes of regimes are governed by an exogenous threshold variable. When the threshold variable increases above or
decreases below a predetermined level the model switches regimes. Statistical tests are then used to verify the number of regimes in the econometric model and each regime is identified as a normal state, state of boom, or a state of bust.

Our approach to identifying various credit regimes requires application of a novel econometric method. Given the short time-series data related to credit markets for individual countries and a limited number of countries with longer time-series data, we found it necessary to conduct estimation methods for panel data using a limited number of observations. The recently introduced methods for estimating dynamic threshold models for panel data rely on the instrumental variable approach (Caner and Hansen, 2004; Kremer, Bick, and Nautz, 2011). They are not explicitly designed for small samples and therefore may provide imprecise estimates of regression parameters.

We estimate the dynamic panel data models using the bootstrap-corrected LSDV (least squares dummy variable) method of Everaert and Pozzi (2007). This method produces more precise and less biased estimates in small samples than other estimation methods. Our analysis is one of the first applications of this method to dynamic threshold regressions for panel data.¹ Using this approach we are able to identify normal and boom regimes in the models of credit to households.

In the next section we describe the method used to identify normal and boom regimes within the credit market. Empirical results are presented in Section 3 and the final section will share our conclusions.

¹ After conducting the estimations we found that Shin and Kim (2011) analyzed a threshold model of Tobin’s Q investment function with the same estimation technique. These authors also investigated the finite sample properties of this estimation method. However, their model assumes only two regimes and does not explicitly control for changes in the constant term between regimes.
2. Identification of multiple regimes for credit growth

Several studies analyze multiple states (or regimes) occurring within credit markets. The most common distinction that exists within the literature is between the credit-rationing regime and the “normal” (demand-driven) regime (Blinder, 1987; Azariadis and Smith, 1998; Balke, 2000). In the former regime the amount of loans distributed to firms and households depends on the supply-side which includes factors related to restrictive lending policies of banks, the interest rate spread, minimum loan to value ratios, and other measures of credit rationing. In the latter regime various demand factors including the lending interest rate, profits of companies, wages, and price of goods all affect the level of credit in the economy.

Another possible regime considered in economic studies is the state of boom. Markets for goods are vulnerable to booms that are driven by rapid and often prolonged growth in demand. Capital markets are afflicted by asset booms or bubbles when investor expectations move stock prices up and away from fundamentals. Similarly, boom periods in the credit market are observed when the demand for loans raises the level of credit beyond the sustainable equilibrium. Credit booms are modeled not only as deviations from that equilibrium but also as separate regimes that can last for some time (e.g., Backé and Wójcik, 2008; Lorenzoni, 2008). Such boom regimes end either with a bust or a soft landing after which credit returns to the long-run equilibrium.

The presence of credit-rationing, sustainable and unsustainable (boom and bust) states provides the rationale for using a multi-regime econometric model to explain the changes in credit to households. The statistical method to test for the presence of two, three or more states of the lending market is discussed below followed by a description of the procedure with which to identify each regime, including the boom regime.

2.1 Econometric modeling of multiple regimes for credit
A popular approach to explain the change in credit in relation to output, $\Delta c$, for country $i$ at time $t$ is to estimate the following error correction model

$$\Delta c_{i,t} = \alpha_i + \beta \cdot ECT_{i,t-1} + \sum_{k=1}^{m} \gamma_k \cdot x_{k,i,t} + \epsilon_{i,t}$$

(1)

where $ECT$ is the error correction term from the long-run regression explaining the ratio of credit to output, $c$. The parameter $\beta$ represents the rate at which credit nears the equilibrium after the occurrence of a shock that has shifted credit away from that established equilibrium, assuming that there are no other factors in play. A negative value of $\beta$ is required for credit to persistently move towards the equilibrium. $x_k$ is the $k$th explanatory variable affecting the credit growth in the short-run. The “fixed effect” parameters $\alpha_i$ control for possible differences in average credit growth between countries.

The formula (1) was used to estimate the equilibrium level of credit and the short-term changes of credit depending on deviations from that equilibrium in some earlier studies. Any possible divergence of credit from theoretical values generated by this model would be considered a boom, a bust, or some other violation of the natural development of credit around the equilibrium such as the process of catching up or stagnation.

Due to the drawbacks of linear error correction models mentioned in the introduction, we propose another method to identify credit booms. Since a boom is defined as a divergence of credit from its equilibrium level, it may be possible to determine if the mechanism described by the error correction model does not function in some periods. There is the potential that there exists a state in the market when credit does not return to the equilibrium but instead it grows rapidly. This would be observable in model (1) if the parameter $\beta$ took a nonnegative value.

We attempt to distinguish between periods of credit divergence from the long-run equilibrium using the following multi-regime threshold regression model
Identification of multiple regimes for credit growth

\[ \Delta c_{i,t} = \begin{cases} 
\alpha_i + \beta^{(1)} \cdot ECT_{i,t-1} + \sum_{k=1}^{m} \gamma_k^{(1)} \cdot x_{k,i,t} + \epsilon_{i,t} & \text{when } z_{t-l} \leq \phi^{(1)} \\
\alpha_i + \beta^{(2)} \cdot ECT_{i,t-1} + \sum_{k=1}^{m} \gamma_k^{(2)} \cdot x_{k,i,t} + \delta^{(1)} + \epsilon_{i,t} & \text{when } \phi^{(1)} < z_{t-l} \leq \phi^{(2)} \\
\vdots & \\
\alpha_i + \beta^{(r)} \cdot ECT_{i,t-1} + \sum_{k=1}^{m} \gamma_k^{(r)} \cdot x_{k,i,t} + \delta^{(r-1)} + \epsilon_{i,t} & \text{when } \phi^{(r-1)} < z_{t-l} 
\end{cases} \quad (2) \]

where the variable \( z_{t-l} \), lagged by \( l \) periods determines the actual regime of the model in each period \( t \). The threshold variable \( z_{t-l} \) may represent the trigger of a boom, as this is the variable that switches regimes of the model between the normal state and the states of boom and bust. The additional parameters \( \delta^{(i)} \) control for possible differences in the average growth of credit between regimes (Bick 2010).

In one or more regimes it is noteworthy that credit follows macroeconomic fundamentals and returns to the equilibrium after possible shocks; however, in some regimes of the model (2) the regression parameters \( \beta, \gamma, \) and \( \delta \) may become more characteristic of a boom. We discuss these issues in the subsection 2.3.

In our empirical analysis we use the estimation techniques developed for the dynamic panel data. Namely, we estimate different specifications of the models (1) and (2) using the bootstrap corrected LSDV estimator developed by Everaert and Pozzi (2007). This estimation method provides precise estimates of regression parameters in small samples (see also Shin and Kim, 2011). A more detailed explanation of this estimation method is presented in Appendix 1.

The estimation procedure also helps to select the optimal threshold variable \( z_{t-l} \) and its lag \( l \). When the number of candidate threshold variables and their lags is a finite integer, the best threshold variable is selected by estimating the threshold regression with each candidate variable separately. The optimal threshold variable is the one that minimizes the sum of the squared residuals in (2).
2.2 Selecting the number of regimes

The presence of multiple regimes is determined using the test developed by Hansen (1999) whereby the null hypothesis assumes no additional regimes in the model explaining changes of credit and there is at least one additional regime according to the alternative hypothesis. We start with the null hypothesis where the correct specification is the linear model (1) and the two-regime model is valid and in line with the alternative hypothesis:

\[ H_0 : \beta^{(1)} = \beta^{(2)} , \gamma_k^{(1)} = \gamma_k^{(2)} , \delta^{(1)} = 0 \] and \[ H_1 : \beta^{(1)} \neq \beta^{(2)} \text{ or } \gamma_k^{(1)} \neq \gamma_k^{(2)} , \text{ or } \delta^{(1)} \neq 0 . \]

The parameter \( \phi^{(1)} \) is not identified under the null hypothesis and therefore the Wald, Lagrange Multiplier, or Likelihood Ratio statistics do not have their standard distributions. As in Hansen (1999), we employ the \( \sup F \) statistic and approximate its distribution under the null using the fixed-regressor bootstrap method.

In the first step we compute the \( F \) statistic using the following formula

\[ F = \frac{SSR_0 - SSR_1}{SSR_1} \cdot n \cdot (T - 1) \]  

where \( SSR_0 \) is the sum of squared residuals from the estimated linear model (1), \( SSR_1 \) is the sum of squared residuals from the estimated threshold model (2) with two regimes, \( n \) is the number of cross sections, and \( T \) is the number of time-series observations.

In the second step we apply a bootstrap procedure to calculate the p-values of the \( F \) statistic. We treat all explanatory variables including the threshold variable as given. We also construct the empirical distribution from residuals of the original estimated two-regime threshold model (2). We then draw (with replacement) elements from this distribution to create a bootstrap sample (bootstrapped values of \( \Delta c_{i,t} \)) under \( H_0 \). The bootstrapped sample is then used to estimate both linear and threshold models with which to calculate the \( F \) statistic (3). The bootstrap procedure is repeated a large number of times to construct the
empirical distribution of $F$. Finally, we compare the original $F$ statistic from the first step with the constructed empirical distribution and calculate the p-value for our test.

When the three-regime model is tested against the two-regime threshold regression, the testing statistic is analogous to (3):

$$F_2 = \frac{SSR_1 - SSR_2}{SSR_2} \cdot n \cdot (T - 1).$$

(4)

The value $SSR_2$ is the sum of squared residuals from the estimated threshold model (2) with three regimes.

The bootstrap procedure may also be used to approximate the distribution of the $F_2$ statistic where bootstrapped samples are constructed under the assumption that the two-regime model is the valid data generating process. A large number of bootstrapped samples are used to estimate the two-regime and three-regime models and to calculate the $F_2$ statistic for each sample. The approximate p-value can be found by comparing the $F_2$ statistic computed from the original data with the empirical distribution of the bootstrapped $F_2$ statistics. Analogously, a larger number of regimes can be examined by using the iterative approach that starts with one regime and increases the number of regimes by one in each step until the null hypothesis is not rejected by the $F$ test.2

2.3 Identifying booms in the credit market

In our threshold error correction model the long-run relationship between credit and other macroeconomic variables does not change between regimes. This means that there exists only one long-term equilibrium state for credit. The short-run parameters and the error correction parameter are used to differentiate between different “transitional states” of the

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2 The power of the tests used here and the uncertainty associated with the estimated models may affect the selected number of regimes. Some appropriate model averaging technique and the identification of separate regimes based on economic theory (discussed in subsection 2.3) may (at least to some extent) help to minimize the bias caused by the wrong decision about the number of regimes for the testing method.
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credit market. Some (at least one) of these transitional states should move credit towards the long-run equilibrium; the other states could potentially allow credit to deviate significantly from that equilibrium for some time.

We assume that each state of the credit market can be represented as a separate regime in the econometric model. The state at which credit moves along the long-run equilibrium would be called the “normal state” or the “sustainable state”. It can be represented in the econometric model by the regime where the value of the error correction parameter \( \beta^{(i)} \) belongs to the region \((-1; 0)\); in this case credit tends to return to the equilibrium after any disturbance. The parameters of the short-run regressors, \( \gamma^{(i)}_k \), are expected to show signs consistent with the economic theory and as such relevant demand and supply factors should be accounted for.

The state of boom can be identified as the regime where \( \beta^{(i)} \geq 0 \); in this case credit tends to diverge or move independently from the long-run equilibrium. Additionally, when the lagged dependent variable is included among regressors, its (autoregressive) parameter is expected to be positive to account for the persistence of positive credit growth. The parameter \( \delta^{(i)} \) should also be positive to allow credit to grow more rapidly during these booms than during normal times. The boom does not preclude the parameters \( \gamma^{(i)}_k \), which conform with the demand factors affecting changes in credit. However, the supply factors are expected to be insignificant. For example, rising housing prices can affect credit to households significantly during credit booms because the rapid credit growth is often associated with a boom in a housing market.

Credit busts are more difficult to identify; they are represented in the threshold error correction model by regimes where credit returns extremely quickly to the sustainable equilibrium. The error correction parameter would be close to \(-1\) and the parameter \( \delta^{(i)} \)
could be negative in such cases. Both short-run supply and demand factors could also play a role here, especially if the busts were initiated by a decrease in the demand for goods, falling prices and more restrictive bank policies. However, some busts and soft landing incidents may be difficult to distinguish from the “normal states” where credit also tends to return to its equilibrium. One distinction rests on the fact that busts typically occur immediately after booms.

3. Empirical results

We used annual data from 21 of the OECD or European Union countries for which the time series on credit to households, housing prices, and other important macroeconomic variables are available.3 The sample used begins in 1995 and ends in 2009.

We investigated a number of macroeconomic variables in our empirical analysis and the selection of variables explaining the level of credit and its changes was based on the literature review (Gourinchas, Valdes, and Landerrechte, 2001, Égert, Backé, Zumer, 2006, Kiss, Nagy, Vonnák, 2006, Mendoza and Terrones, 2008). In particular, the variables selected fit the theoretical and empirical analyses of Rubaszek and Serwa (2011). Typically, credit to households is measured in relation to the nominal GDP of each country and in each period. The explanatory variables usually considered in empirical studies of credit to households include the GDP per capita (or some other measure of disposable income), the market interest rates, the loan-deposit interest rate spread (as a measure of lending policies of the banks), the unemployment rate and the long-run unemployment rate (as measures of income uncertainty and persistence), and the housing price index (to account for the loan-to-value limits in housing loans).

3 The investigated countries include: Australia, Austria, Belgium, Bulgaria, Canada, Denmark, France, Germany, Greece, Italy, Japan, Netherlands, New Zealand, Norway, Portugal, South Korea, Spain, Sweden, Switzerland, the United Kingdom, and the United States of America.
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After a careful robustness check, we chose only those variables that remained significant in different model specifications (i.e. they were significant in the dynamic linear models and in at least one regime of the threshold regression models). We found that the significant variables explaining the level of credit in relation to GDP were the interest rate spread, the level of GDP per capita, and the housing price index. All variables were computed in natural logarithms.

3 The investigated countries include: Australia, Austria, Belgium, Bulgaria, Canada, Denmark, France, Germany, Greece, Italy, Japan, Netherlands, New Zealand, Norway, Portugal, South Korea, Spain, Sweden, Switzerland, the United Kingdom, and the United States of America.
Given the limitation of the data, all variables (household loans) have been constructed to be consistent in time to a maximum extent; however, some differences in definitions between countries are possible. The sources of data for variables used in our final models are as follows: the value of loans supplied to households was provided in nominal terms and the data came from the OECD, BIS Data Bank, ECB, international central bank databases, and Ecowin; the data for the nominal GDP and the GDP per capita at constant prices was taken from the World Bank WDI database; finally, the interest rate spread was determined as the approximate difference between the lending rate (usually the rate on housing loans or the rate for primer customers) and the deposit rate. The data for the lending and deposit rates came from the BIS Data Bank, ECB, and IMF IFS databases. The housing price indices (HPI) were constructed using data from the BIS Data Bank, national central banks and statistical offices, and from the Global Property Guide internet database.

We estimated the long-run relationship between the analyzed variables using the continuously-updated fully-modified (CupFM) estimator of Bai, Kao, and Ng (2009). This estimation method controls for possible common factors between cross-sections in the panel data, e.g. common trends or business cycles. The test provided by Bai, Kao, and Ng suggests that the correlation between cross-sections is indeed statistically significant.

<table>
<thead>
<tr>
<th>Table 1: Long-run dependence between credit and other macroeconomic variables</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parameter value</td>
</tr>
<tr>
<td>Spread</td>
</tr>
<tr>
<td>GDP per capita</td>
</tr>
<tr>
<td>hpi</td>
</tr>
<tr>
<td>F statistic</td>
</tr>
</tbody>
</table>

Note: The F statistic verifies the null hypothesis which is that the correlation between cross-sectional panels is equal to zero against the alternative of significant cross-sectional interdependence.
The results presented in Table 1 suggest that the one percentage point increase in the loan-deposit interest rate spread lowers the equilibrium level of credit (in relation to GDP) by 4.5 percent. Similarly, a one percent increase in GDP per capita denotes a higher ratio of credit to GDP by 2.3 percent whereas a one percent increase in the housing price index causes the credit to households (in relation to GDP) to increase by 0.5 percent. We interpret the residual term from this long-run regression as a deviation of credit from the equilibrium level and employ this residual as an error correction term ($ECT$) in our dynamic panel data models.

In the next step, we estimate single and multi-regime error correction models. Given the limited number of observations we have restricted our specifications to account for up to three regimes. The estimated parameters for single and two-regime models are presented in Table 2.

In the single regime model the error correction term is a significant variable; however, its parameter denoting the estimated rate of return to the long-run equilibrium is relatively low ($-0.1$). This suggests that any shock that shifts credit away from the equilibrium may have a prolonged effect. The other variables affecting change in credit to households are the lagged changes in credit, changes in the housing price index and changes in the loan-deposit interest rate spread.

The alternative specifications are the dynamic threshold models with the same explanatory variables but the different threshold variables. The value of the threshold variable identifies the current regime of the model at each period. In the analysis it is useful to employ such threshold variables that could act as potential triggers for credit booms. We used the growth rate of credit to GDP ratio lagged by one period, the growth rate of housing prices lagged by one period, the error correction term lagged by one period, and the level of credit to GDP ratio lagged by one period.\(^4\)

\(^4\) The threshold variables need to be exogenous and stationary. Therefore, results employing the threshold variable $c_{t-1}$ should be treated with some caution.
Note: the explained variable is the growth rate of credit in relation to GDP and the names of the explanatory variables are given in the first column. The columns denoted “param.” consist of parameter estimates and the columns denoted “Std” contain the standard deviations of estimated parameters computed using the bootstrap method. The standard deviation cannot be computed for $\phi$, therefore we present the 95%-confidence region for $\phi$ under its point estimate. The rows denoted “$\text{var}(\epsilon)$” contain estimated residual variances for each model multiplied by one thousand. The asterisks “*”, “**” and “***” denote the statistical significance of variables at the 10%, 5% and 1% levels, respectively. The F statistic is from the Hansen (1999) test of the null hypothesis assuming no threshold effects, thus the single-regime model is valid. The alternative hypothesis assumes that the two-regime threshold model is valid. The asterisks “***” denote rejection of the null hypothesis at the 1% level of significance.
In the model with the lagged credit growth rate acting as a threshold variable, the regimes change when the growth rate of credit increases above or falls below the rate of 9.4 percent of annual growth. This threshold level is rather high. If credit growth is extremely rapid in one period it will tend to follow the macroeconomic fundamentals and return slowly to the equilibrium in the next period. In the other regime, credit is not significantly affected by changes in the interest rate spread (approximating lending policies of banks) and returns to the equilibrium even more slowly. In both regimes changes in the housing price index are most strongly correlated to changes in credit; this suggests that housing loans constitute a significant portion of loans to households in the analyzed countries. There is no evidence of credit boom regimes in this specification.

When the changes in HPI are used as the threshold variable, the following interpretation holds. In the first regime, corresponding to an annual rate of growth of HPI lower than 11.8 percent, credit returns very slowly to its equilibrium and does not react to short-run changes in the spread. The error correction parameter is statistically different from zero only at the 10% level of significance. In addition, there is some persistence in the growth rate of credit in the first regime since the autoregression parameter equals 0.2. These results may point to some weak evidence of a boom in the first regime. In the second regime, the credit returns to the equilibrium five times more quickly than in the first regime; moreover, it also reacts more strongly to short-run changes in the spread and in the HPI.

In the other two models where the error correction term and the level of credit act as the threshold variables, we find a slow adjustment of credit to the long-run equilibrium in most regimes. The strong impact of the error correction term on credit is present only in the first regime of the model with the $ECT_{t-1}$ threshold variable.
This result can be interpreted in the following way: when credit falls too low (more than 13 percent) below the equilibrium level, there is a strong force pushing it back to that equilibrium. This force vanishes however when credit is close or above the equilibrium. Also, changes in the interest rate spread are insignificant in the second regime of both models suggesting that only demand factors affect credit in that state. Again, no boom regimes can be identified here.

All two-regime models are superior to the single-regime regression according to the measure of residual variance; this is in line with the results of Hansen’s (1999) F test. The values of the respective F statistics are presented in Table 2. Interestingly, the optimal two-regime model with a given set of explanatory variables is the one with the lagged ratio of credit to GDP acting as the threshold variable.5

We have presented the results from analogous three-regime models in Table 3. As expected, one additional regime decreases the value of the residual variance in each respective model. The F statistics also reject the null hypothesis of two regimes in favor of the alternative three regimes in all cases, except the model with the $c_{t-1}$ threshold variable where the two-regime specification is not rejected. The optimal threshold variable in the three-regime model is represented by the lagged changes in credit to households $\Delta c_{t-1}$.

The test results are important as they suggest that the three-regime model provide an overall better description of changes with credit to households than the two-regime model. Interpretation of the preferred three-regime models is essential for the identification of possible boom and/or bust periods within the credit markets.

5 According to Hansen (1999) the optimal model is the one with the lowest residual variance or equivalently with the largest value of the F statistic.
Interpretation of the preferred three-regime models is essential for the identification of possible boom and/or bust periods within the credit markets.

Table 3: Estimates of the three-regime models of credit growth

<table>
<thead>
<tr>
<th>Threshold variable</th>
<th>( \Delta c_{t-1} )</th>
<th>( ECT_{t-1} )</th>
<th>( \Delta hpi_{t-1} )</th>
<th>( c_{t-1} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \Delta c_{t-1} )</td>
<td>param.</td>
<td>Std</td>
<td>param.</td>
<td>Std</td>
</tr>
<tr>
<td>1. regime</td>
<td>-0.146 (0.052) **</td>
<td>-0.046 (0.049)</td>
<td>0.484 (0.055) ***</td>
<td>0.085 (0.045) *</td>
</tr>
<tr>
<td>( ECT_{t-1} )</td>
<td>-0.105 (0.044) **</td>
<td>-0.392 (0.111) ***</td>
<td>-0.053 (0.033)</td>
<td>-0.075 (0.028) ***</td>
</tr>
<tr>
<td>( \Delta spread )</td>
<td>0.687 (0.782)</td>
<td>-1.835 (0.555) ***</td>
<td>-0.049 (0.572)</td>
<td>-2.703 (0.550) ***</td>
</tr>
<tr>
<td>( \Delta hpi )</td>
<td>0.384 (0.091) ***</td>
<td>0.284 (0.094) ***</td>
<td>0.435 (0.090) ***</td>
<td>0.620 (0.062) ***</td>
</tr>
<tr>
<td>( \delta_1 )</td>
<td>-0.004 (0.012)</td>
<td>0.044 (0.024) *</td>
<td>0.013 (0.010)</td>
<td>0.007 (0.019)</td>
</tr>
<tr>
<td>2. regime</td>
<td>0.640 (0.213) ***</td>
<td>0.441 (0.087) ***</td>
<td>-0.087 (0.089)</td>
<td>-0.042 (0.184)</td>
</tr>
<tr>
<td>( ECT_{t-1} )</td>
<td>-0.030 (0.031)</td>
<td>-0.052 (0.056)</td>
<td>-0.065 (0.037) *</td>
<td>-0.120 (0.067) **</td>
</tr>
<tr>
<td>( \Delta spread )</td>
<td>-0.271 (0.446)</td>
<td>0.240 (0.497)</td>
<td>0.259 (0.555)</td>
<td>-0.425 (0.894)</td>
</tr>
<tr>
<td>( \Delta hpi )</td>
<td>0.107 (0.056) **</td>
<td>0.217 (0.058) ***</td>
<td>0.284 (0.075) ***</td>
<td>0.247 (0.133) *</td>
</tr>
<tr>
<td>( \delta_2 )</td>
<td>-0.004 (0.012)</td>
<td>0.044 (0.024) *</td>
<td>0.013 (0.010)</td>
<td>0.007 (0.019)</td>
</tr>
<tr>
<td>3. regime</td>
<td>-0.077 (0.095)</td>
<td>0.144 (0.102)</td>
<td>0.133 (0.070) *</td>
<td>0.352 (0.129) ***</td>
</tr>
<tr>
<td>( ECT_{t-1} )</td>
<td>-0.102 (0.035) ***</td>
<td>-0.237 (0.112) **</td>
<td>-0.237 (0.055) ***</td>
<td>-0.061 (0.036) *</td>
</tr>
<tr>
<td>( \Delta spread )</td>
<td>-3.027 (0.583) ***</td>
<td>-1.853 (0.859) **</td>
<td>-1.913 (0.675) **</td>
<td>0.124 (0.430)</td>
</tr>
<tr>
<td>( \Delta hpi )</td>
<td>0.655 (0.074) ***</td>
<td>0.433 (0.093) ***</td>
<td>0.565 (0.083) ***</td>
<td>0.157 (0.063) **</td>
</tr>
<tr>
<td>( \delta_2 )</td>
<td>0.029 (0.017)</td>
<td>0.078 (0.035) **</td>
<td>-0.040 (0.017) **</td>
<td>-0.027 (0.018) *</td>
</tr>
</tbody>
</table>

Threshold \( \phi_1 \) 95%-confidence region for \( \phi_1 \) [-0.001 : 0.037] [-0.132 : -0.132] [-0.004 : 0.051] [-1.062 : -0.509]

Threshold \( \phi_2 \) 95%-confidence region for \( \phi_2 \) [0.078 : 0.099] [0.037 : 0.126] [0.042 : 0.118] [-0.526 : -0.103]

\( \text{var}(\epsilon) \) 1.501 1.631 1.614 1.623

\( F \) statistic 36.57 *** 20.80 * 29.86 ** 8.52

Note: see Table 2. In the last row, the Hansen (1999) F test assumes that two regimes are valid under the null hypothesis and that three regimes are suitable under the alternative. The asterisks “*”, “**” and “***” denote rejection of the null hypothesis at the 10%, 5% and 1% levels, respectively.
In some specifications of the three-regime model it is possible to identify the states most likely resembling periods of a credit boom. The error correction term is insignificant in these regimes and credit does not return to the equilibrium. One such regime is present in the superior model with the lowest residual variance where $\Delta c_{t-1}$ is the threshold variable. This model enters the boom regime when the credit-output ratio grew at the rate between 1.2 and 9.4 percent one period earlier. Interestingly enough, this regime is also characterized by the strong persistence of credit growth and no immediate reaction to changes in the interest rate spread. A similar boom regime is present in the second model (presented in the second column of Table 3) in periods when the threshold variable $ECT_{t-1}$ indicates only small deviations of credit from the equilibrium, between $-13$ and $+12$ percent.

Another interesting result is that there is a stronger tendency for credit to return to the equilibrium when credit grows at the rate greater than 9.4 percent or the deviation of credit from the equilibrium is larger than 12 percent.

In the third model, where the threshold variable is $\Delta hpi_{t-1}$, the tendency for the credit to return to the long-run trend is the weakest in the first regime and is the strongest in the third regime when house prices grow slowly ($\Delta hpi_{t-1} < 0.045$) and rapidly ($\Delta hpi_{t-1} \geq 0.118$), respectively, just one year earlier. At the same time there is a strong correlation between credit change and the housing price index. Therefore, a credit bust is possible in this regime but it requires a simultaneous decline in the price of houses.

The fourth three-regime model, where the threshold variable is $c_{t-1}$, does not explain credit to households significantly better than the two-regime model that is presented in Table 2.
4. Conclusions

The results of our empirical analysis provide important information about the possible triggers of a credit boom. We found that the growth rate of credit to households above the rate of economic growth can be a sign of a future boom. Extremely rapid growth of house prices or credit may lead to a regime where credit quickly returns to its equilibrium. Booms also often follow periods where credit does not deviate too strongly from the long-run trend.

The method proposed by this study may be useful in identifying other types of booms (housing booms, asset bubbles) or to detect periods where some economic variables deviate from their long-run trends or equilibria. While the time-series methods to identify multiple regimes require a large number of consecutive observations, our panel data approach utilizes a limited number of time-series observations from several countries or other cross-sectional units.

Possible extensions of our model include: (1) enabling regime changes affected by a set of variables instead of a single variable in order to enrich the economic interpretation of the model, (2) specifying threshold vector error correction models to account for possible bilateral links between macroeconomic variables, (3) applying Markov chains to explain the changing regimes of the models – in order to calculate the probability of regime changes. A similar approach may also be used to identify regimes for credit supplied to firms or for other types of loans.
References


Appendix 1: The bootstrap-based bias correction method for estimating threshold error correction models for panel data.

We begin by describing the procedure to estimate the following linear error correction model

\[
\Delta y_{i,t} = \alpha_i + \beta \cdot (y_{i,t-1} - x_{i,t-1} \hat{b} - \hat{\lambda}_i) + w_{i,t} \gamma + e_{i,t} \tag{A.1}
\]

where \( \Delta y_{i,t} \equiv y_{i,t} - y_{i,t-1} \), \( x \) is the vector of explanatory variables in the long-run relationship and \( w \) is the vector of variables including \( \Delta y_{i,t-1} \) explaining the short-run changes in \( y \). The error term \( e_{i,t} \) is independent and identically distributed with mean zero and finite variance \( \sigma_e^2 \). The parameters \( \beta \), \( \hat{b} \), and \( \gamma \) take on common values for different cross sections whereas \( \alpha_i \) and \( \hat{\lambda}_i \) are the fixed-effects parameters in the short-run and long-run relationships, respectively.

In the first step we estimate the cointegration relationship between the dependent variable \( y \) and the vector \( x \). In our case, we employed the method of Bai, Kao, and Ng (2009) to control for potential cross-sectional correlation (i.e. common global stochastic trends) in the panel data.

The error correction term for the country \( i \) and the period \( t \) is estimated as a residual from cointegration relation

\[
ect_i = y_{it} - \hat{b} \cdot x_{it} - \hat{\lambda}_i. \tag{A.2}
\]

In the second step we estimate the vector of parameters \( \theta \equiv (\beta, \gamma) \) of the error correction model using the method described by Everaert and Pozzi (2007). This method corrects bias in parameters estimated with the least squares dummy variable (LSDV) method, \( \hat{\theta}_{\text{LSDV}} \equiv (\hat{\beta}_{\text{LSDV}}, \hat{\gamma}_{\text{LSDV}}) \). The bootstrap procedure simulates the distribution of the LSDV
estimator by sampling from (A.1) as well as some vector of parameters $\tilde{\theta} \equiv (\tilde{\beta}, \tilde{\gamma})'$ and returns the mean bootstrap estimate $\hat{\theta}_b \equiv (\hat{\beta}_b, \hat{\gamma}_b)'$ as explained in detail by Everaert and Pozzi (2007). A simple iteration procedure is used to find such a vector $\tilde{\theta}$ that generates the mean bootstrap estimate $\hat{\theta}_b$ equal to the original biased LSDV estimate $\hat{\theta}_{LSDV}$. The final estimate of $\theta$ is $\tilde{\theta}$ for which $\hat{\theta}_b = \hat{\theta}_{LSDV}$.

The same procedure can be used to estimate the threshold error correction model with $R$ regimes:

$$\Delta y_{i,t} = \begin{cases} \alpha_t + \beta(1) \cdot (y_{i,t-1} - x_{i,t-1} - \lambda_t) + w_{i,t} \gamma(1) + \epsilon_{i,t} & \text{when } z_t \leq \phi(1) \\ \alpha_t + \beta(2) \cdot (y_{i,t-1} - x_{i,t-1} - \lambda_t) + w_{i,t} \gamma(2) + \delta(1) + \epsilon_{i,t} & \text{when } \phi(1) < z_t \leq \phi(2) \\ \vdots & \vdots \\ \alpha_t + \beta(R) \cdot (y_{i,t-1} - x_{i,t-1} - \lambda_t) + w_{i,t} \gamma(R) + \delta(R-1) + \epsilon_{i,t} & \text{when } \phi(R-1) < z_t \end{cases} \quad \text{(A.3)}$$

where the vector of short-run parameters $\theta(r) \equiv (\beta(r), (\gamma(r))')'$ alternate their values between regimes, but the long-run parameters $\mathbf{b}$ and the fixed effects $\alpha_t$ and $\lambda_t$ remain constant throughout all regimes. The term $\epsilon_{i,t}$ is assumed to be independent and identically distributed with zero mean and finite variance $\sigma^2_{\epsilon}$.

When the values of the threshold parameters $\phi(1), \phi(2), \ldots, \phi(R)$ are known, the threshold regression (A.3) can be easily transformed into the linear model

$$\Delta y_{i,t} = v_{i,t}^{(1)} \beta^{(1)} + v_{i,t}^{(2)} \beta^{(2)} + \ldots + v_{i,t}^{(R)} \beta^{(R)} + \sum_{r=1}^{R} \alpha^{(r)} \mathbf{I}^{(r)} + \sum_{r=2}^{R} \delta^{(r-1)} \mathbf{I}^{(r)} + \epsilon_{i,t} \quad \text{(A.4)}$$

where $\mathbf{I}^{(r)} \equiv I(\phi^{(r-1)} \leq z_t < \phi^{(r)})$ is the indicator variable taking on 1 in the regime $r$ (i.e. when $\phi^{(r-1)} \leq z_t < \phi^{(r)}$, and 0 otherwise; $v_{i,t}^{(r)} \equiv v_{i,t} \cdot \mathbf{I}^{(r)}$ and $v_{i,t} \equiv (ect_{i,t}, w_{i,t})$). The formula (A.4) is a dynamic linear regression model and can be estimated with the bias-corrected LSDV method of Everaert and Pozzi (2007).
Our method of estimating threshold regressions with unknown values of the threshold parameters $\phi^{(1)}$, $\phi^{(2)}$, ..., $\phi^{(R)}$ is similar to the method proposed by Hansen (1999) for non-dynamic panel threshold regressions. We start with a two-regime model and estimate its parameters by guessing the value of $\phi^{(1)}$, transforming the parameters into the linear model (A.4) and using the method of Everaert and Pozzi (2007) to obtain parameters $\theta^{(r)} = (\beta^{(r)}, (\gamma^{(r)})')'$ from each regime. The estimate of $\phi^{(1)}$ is found using a grid search over the set $G$. $G$ is the set of all observation values of the threshold variable $z_t$ in the sample constrained by 15% of the highest and 15% of the lowest observation values. For each guess of the $\phi^{(1)}$ value we estimate the parameters $\theta^{(1)}$ and $\theta^{(2)}$ of the threshold model and compute the residual variance $\text{var}(\varepsilon)$. The estimates of $\phi^{(1)}$, $\theta^{(1)}$, $\theta^{(2)}$ are those that minimize the value of $\text{var}(\varepsilon)$.

For the three-regime model we use the estimate of $\phi^{(1)}$ from the two-regime model and determine the estimate of $\phi^{(2)}$ using the grid search method described above. The minimum allowed distance between the estimated values of $\phi^{(1)}$ and $\phi^{(2)}$ is imposed in such a way that none of the regimes consists of less than 15% of the observations in the sample. The estimates of $\phi^{(1)}$, $\phi^{(2)}$, $\theta^{(1)}$, $\theta^{(2)}$, $\theta^{(3)}$ are those that minimize the value of $\text{var}(\varepsilon)$. An analogous iterative procedure can be used to estimate threshold models with a larger number of regimes.